

Consider the universal Relation $R = \{A, B, C, D, E, F, G, H, I, J\}$ and the set of Functional dependencies
 $F = (\{A, B\} \rightarrow \{C\}, A \rightarrow \{D, E\}, \{B\} \rightarrow \{F\}, \{F\} \rightarrow \{G, H\}, \{D\} \rightarrow \{I, J\})$

Answer :- First understand the Definition of 2NF

2NF Says that Non prime attribute should fully functionally dependent on the candidate key (prime attribute)

1st step :- Find the candidate key, and prime attributes and Non prime attributes list down all the functional dependencies given in the problem.

$\{A, B\} \rightarrow C$ $A \rightarrow \{D, E\}$ $\{B\} \rightarrow \{F\}$ $F \rightarrow \{G, H\}$ $D \rightarrow \{I, J\}$	}	AB is not present in the RHS
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Identify the attributes which is not present in the RHS of the dependencies (AB)

Find the closure of AB

$$(AB)^+ = ABCDEFGHIJ$$

AB is the candidate key \therefore you can reach all the attributes through AB.

\therefore AB is a ~~candidate~~ candidate key.

prime Attributes are A and B

Non prime Attributes are C, D, E, F, G, H, I, J

Decompose the Relation based on the PA

$R_1 (A, B, C) \quad AB \rightarrow C$

$R_2 (A, D, E, I, J) \quad A \rightarrow \{D, E, I, J\}$

$R_3 \{B, F, G, H\} \quad B \rightarrow \{F, G, H\}$

$\therefore R_1, R_2,$ and R_3 contain NO partial dependencies

So they are in 2NF

However R_2 and R_3 are still an issue because they contain transitive dependencies

① $A \rightarrow \{D, E\}$
 $D \rightarrow \{I, J\}$ } ~~R_{2a}~~ $R_{2a} (D, E)$
 $R_{2b} (D, I, J)$

② $B \rightarrow F$
 $F \rightarrow G, H$ } $R_{3a} (B, F)$
 ~~R_{3b}~~ $R_{3b} (F, G, H)$

The above dependencies are in 3NF

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